

**“Common core” standards,  
student test scores  
in math computation  
in some mid-Atlantic states  
and the implications for  
chemistry instruction**

Presented 5/12/2011 to the  
ACS Mid-Atlantic Regional Meeting in College Park, MD  
By Rick Nelson, Retired Instructor  
EANelson@ChemReview.Net

Q: How can we improve achievement and retention in initial chem courses?

NCTM standards = ?

# In my view,

(Vote for ONE:)

For the current generation of students in **first**-year chem, ***math background*** is:

- A. Not a problem
- B. A minor problem
- C. A major problem

Vote for ONE:

To be *prepared* for first-year Chem, it is *most* important for students to have background knowledge in

- A. Total Math – math of all types
- B. Math Reasoning
- C. Math Computation

$$\begin{aligned}\mathcal{E} &= \mathcal{E}_{\text{cell}}^{\circ} - \frac{0.0591}{n} \log(Q) \\ &= 1.76 - \frac{0.0591}{2} \log \left( \frac{[\text{Zn}^{2+}][\text{VO}^{2+}]^2}{[\text{VO}_2^+]^2[\text{H}^+]^4} \right) \\ &= 1.76 - \frac{0.0591}{2} \log \left( \frac{(1.0 \times 10^{-1})(1.0 \times 10^{-2})^2}{(2.0)^2(0.50)^4} \right) \\ &= 1.76 - \frac{0.0591}{2} \log (4 \times 10^{-5}) = 1.76 + 0.13 = 1.89 \text{ V}\end{aligned}$$

-- Zumdahl, 5<sup>th</sup> edition

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-- Brown, Lemay, 8th Ed. p. 368

THUS

$$u_{\text{rms}} = \sqrt{\frac{3 \left( 8.3145 \frac{\text{J}}{\text{K} \cdot \text{mol}} \right) (298 \text{ K})}{4.00 \times 10^{-3} \frac{\text{kg}}{\text{mol}}}} = \sqrt{1.86 \times 10^6 \frac{\text{J}}{\text{kg}}}$$

Since the units of J are  $\text{kg} \cdot \text{m}^2/\text{s}^2$ , this expression becomes

$$\sqrt{1.86 \times 10^6 \frac{\text{kg} \cdot \text{m}^2}{\text{kg} \cdot \text{s}^2}} = 1.36 \times 10^3 \text{ m/s}$$

-- Zumdahl, 5<sup>th</sup> Ed. p. 218

Vote for ONE:

In first-year Chem, it is *most* important for students to have background knowledge in

- A. Total Math – all types
- B. Math Reasoning
- C. Math Computation

In chem, which one is MOST important?

# For $\sim 10^+$ year faculty:

(Vote for ONE:)

During the past **10 years**, I have seen the ***computation skills*** of first-year students:

- A. Improve substantially
- B. Improve
- C. Not change
- D. Decline
- E. Decline substantially

- What's the problem?
- Why the problem?
- How can we fix the problem?

# Maryland: Math Remediation

Among MD HS students who took the SAT or ACT in 2008 and who enrolled in MD public colleges or universities:

- **Core** students = 3 years of HS Math and 2 years of HS science; **Non-core** students = not.

A *remedial math* course in college was needed by

- **32% of core students** and 49% of non-core students.

Including, at University of Maryland system campuses

- 14% of core students and 27% of non-core students.

And at MD community colleges

- 56% of core students and 69% of non-core students.

- **Virginia**
- **Statewide Remediation**
- Graduated at a Virginia HS, enrolled in remedial MATH in **VA** college:
  - 2002: 17%
  - 2010: 18%

-source: SCHEV

# Virginia Math Results:

- Stanford 9 standardized test given statewide
- National percentile average = 50 on 1995 norms

VA all students	Grade 9				
	1998	1999	2000	2001	2002
Total Math	54	55	55	55	55

Two **subtests** were reported described as

- “**Math Problem Solving**, which focuses on **reasoning** skills, and
- **Math Procedures**, which measures the student’s facility with **computation**.”

# Virginia Math Test Scores

VA Stanford 9	Grade 9				
	1998	1999	2000	2001	2002
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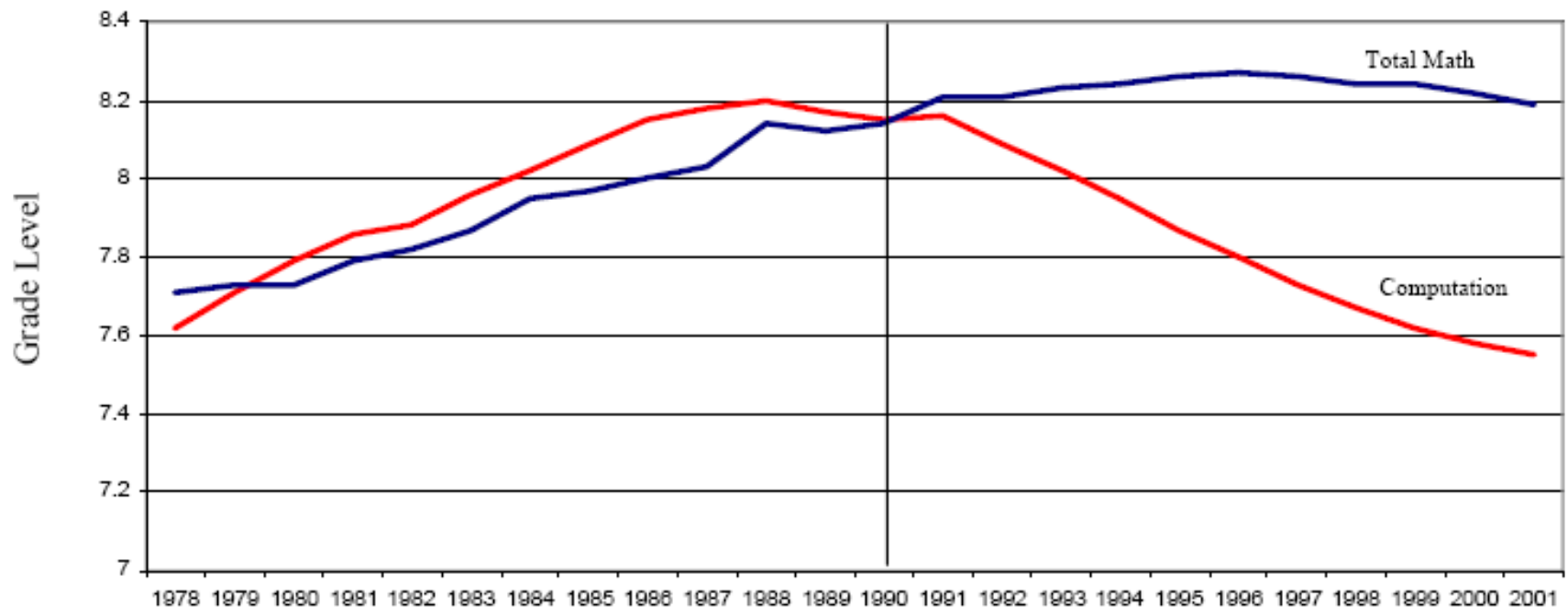
Evidence: (from sample of 80,000 students)

- They were learning SOME math! But not math needed for science
- Reasoning did not help with computation: No transfer.
- “Total Math” scores tell nothing about reasoning and computation.
- 39<sup>th</sup> percentile = Not many ready for chemistry.
- Why these results?
- Do Virginia results apply to other states?

Next three slides from:

Tom Loveless  
Brown Center on Education Policy  
of the Brookings Institution  
Presentation on Math Reform  
at AEI March 4, 2002

# ITBS 8th Grade State of Iowa, 1978-1999



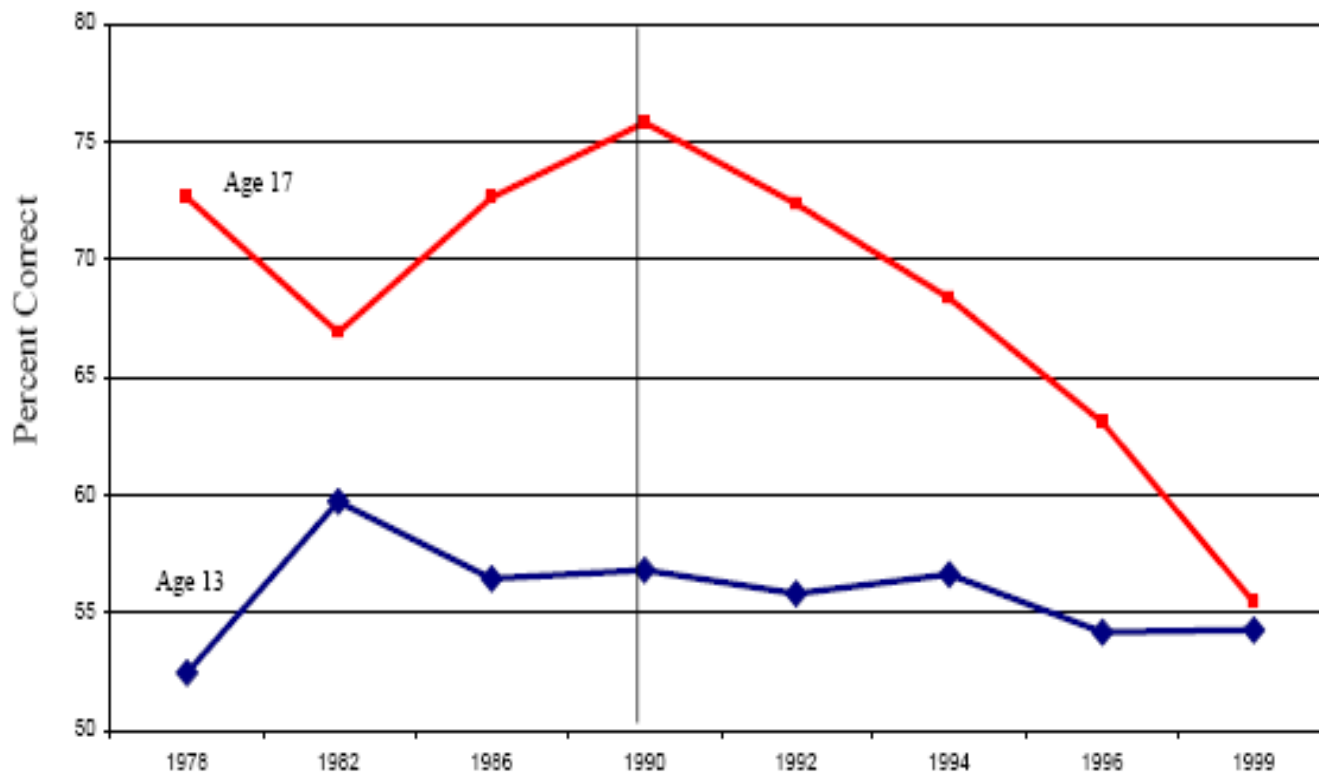
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# Fractions-- Item Analysis

## NAEP Long-Term Trend, 1978-1999



Fraction data taken from NAEP 1999 Long-term trend Mathematics Summary Data Tables

$$\begin{aligned} \mathcal{M} &= \frac{dRT}{P} \\ &= \frac{(3.09 \text{ g/L})(0.0821 \text{ L-atm/mol-K})(304 \text{ K})}{(735/760) \text{ atm}} \\ &= 79.7 \text{ g/mol} \end{aligned}$$

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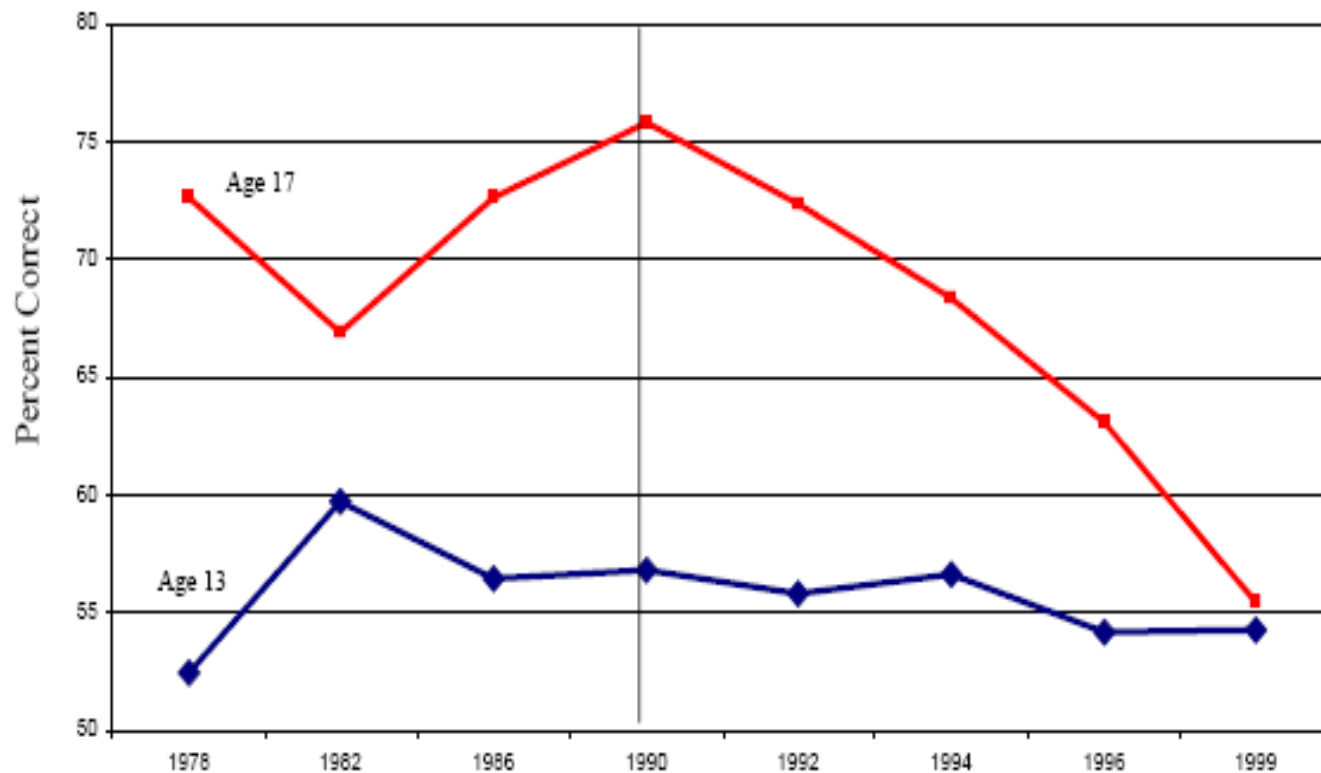
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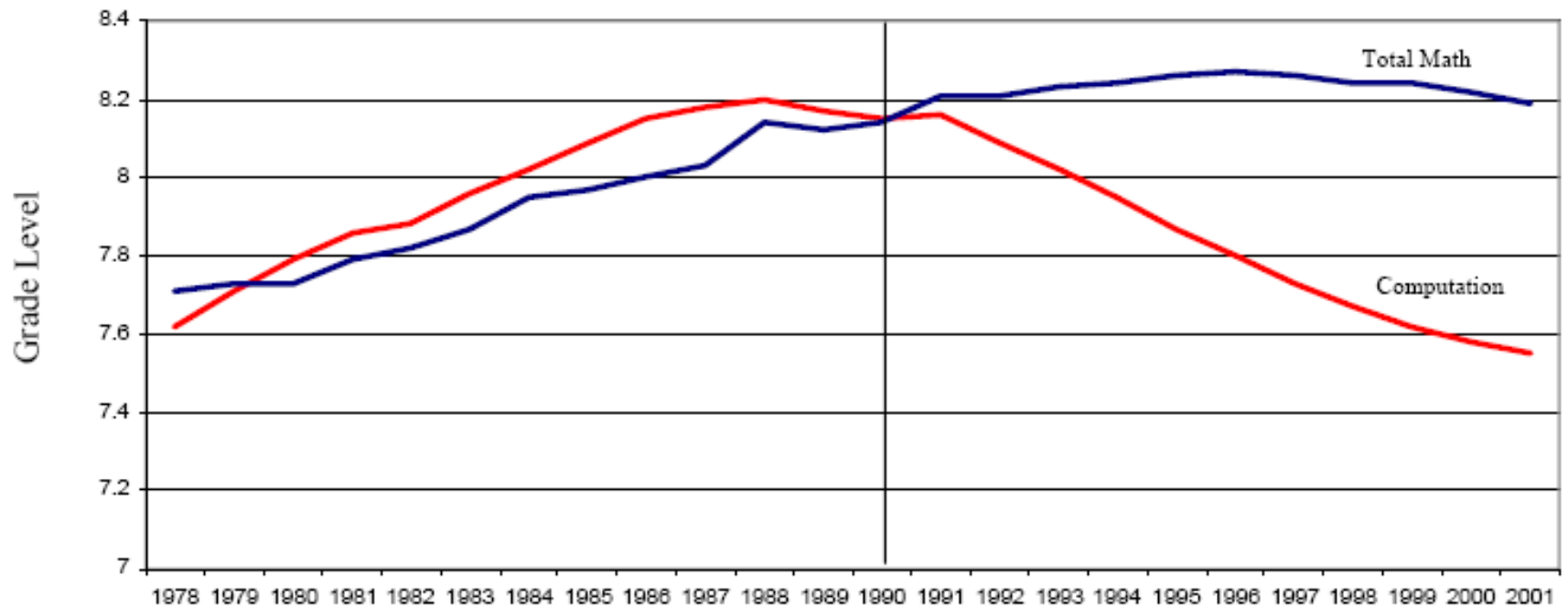


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In Preparation for Chem  
is “**Math**” the problem?

The evidence is: **No.**

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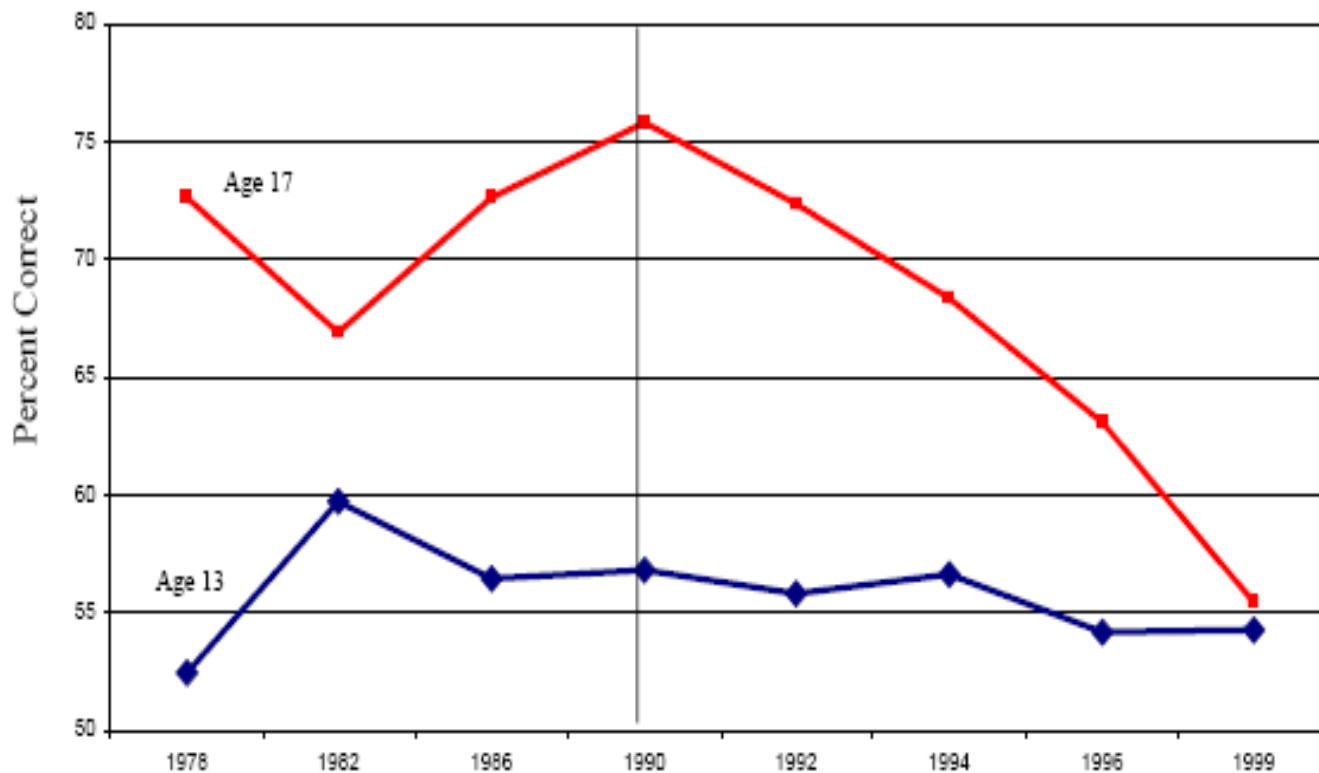
The problem is  
computation.

# Implications for Chem Depts?

- It's not 1990

# Fractions-- Item Analysis

## NAEP Long-Term Trend, 1978-1999



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# Implications for Nation?

# In ~1990, **Why** the Change?

“The **1989** NCTM standards played the role of national standards....

Nearly all state standards after 1990 were modeled on the *1989 NCTM Standards*.”

-- from **Computation Skills, Calculators, and Achievement Gaps: An Analysis of NAEP Items**  
Tom Loveless, The Brookings Institution, April 2004

# The Math Wars

Short history:

## **A quarter century of US 'math wars' and political partisanship**

David Klein

California State University, Northridge

<http://www.csun.edu/~vcmth00m/bshh.html>

longer version:

<http://www.csun.edu/~vcmth00m/AHistory.html>

# NCTM's *An Agenda for Action* (1980):

- “All students should have access to **calculators** and increasingly to computers **throughout** their school mathematics program.”

# New Jersey

## -- Current Math Standards

### **STANDARD 5 — TOOLS AND TECHNOLOGY**

#### **K-12 Overview**

All students will regularly and routinely use calculators, computers, manipulatives, and other mathematical tools to enhance mathematical thinking, understanding, and power.

# NJ: Use Calculators in 1<sup>st</sup> Grade

- Q and A  
Core Standards in Mathematics  
NJ State Board of Education – 2002 to current
- Q: The standard says that students will "use calculators as problem-solving tools...." For what grade levels is this a reasonable expectation?
- A: **Calculators** can and should be used at **all grade levels** .... The majority of questions on New Jersey's new **third-** and fourth-grade **assessments** in mathematics will assume student access to at least a four-function calculator.

-- <http://www.state.nj.us/education/frameworks/math/math3.pdf>

# To Balance:



Use a calculator?

# *1989 NCTM Standards*

Recommended for “**INcreased** attention” were

In Grades 5-8:

- “**Reasoning** inductively and deductively”
- “**Creating algorithms** and procedures”

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In Grades 5-8:

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# 1989 NCTM Standards

Recommended for “**decreased** attention” were

- “Memorizing rules and algorithms”,
- “Finding exact forms of answers”
- “Manipulating symbols”
- “Relying on **outside authority** (teacher or answer key)”
- “Rote **practice**”
- “Paper and pencil **fraction** computation”,

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Was this  
taken  
seriously?

“By 2000, all but two states ... modeled their own curriculum **standards** on the NCTM’s, and publishers revised math **textbooks** to conform with NCTM’s prescriptions.”

-- from

**Computation Skills, Calculators, and  
Achievement Gaps:**

**An Analysis of NAEP Items**

Tom Loveless, The Brookings Institution, April 2004

- Take a look at K-12 math books.
- See how much content is preparation for scientific calculations.

# Results Make Sense?

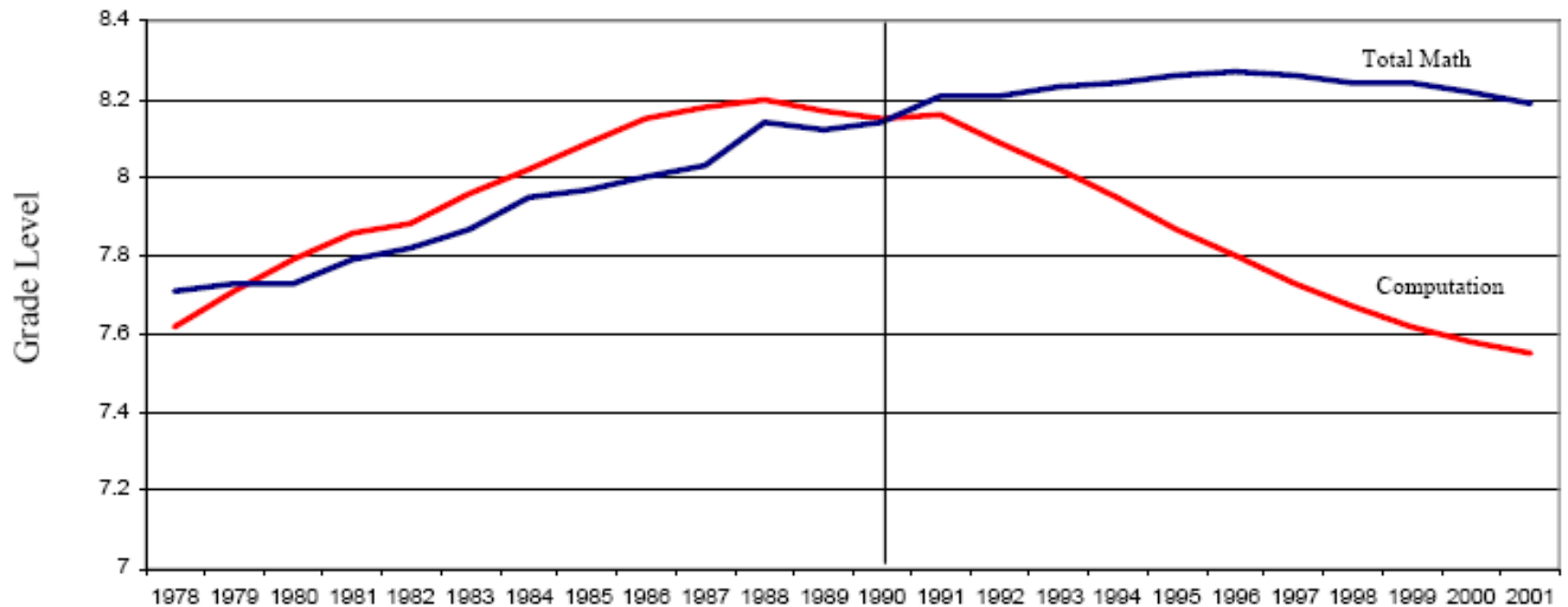
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Why no computation  
data since 2002?

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# 2003: Computation Data STOP

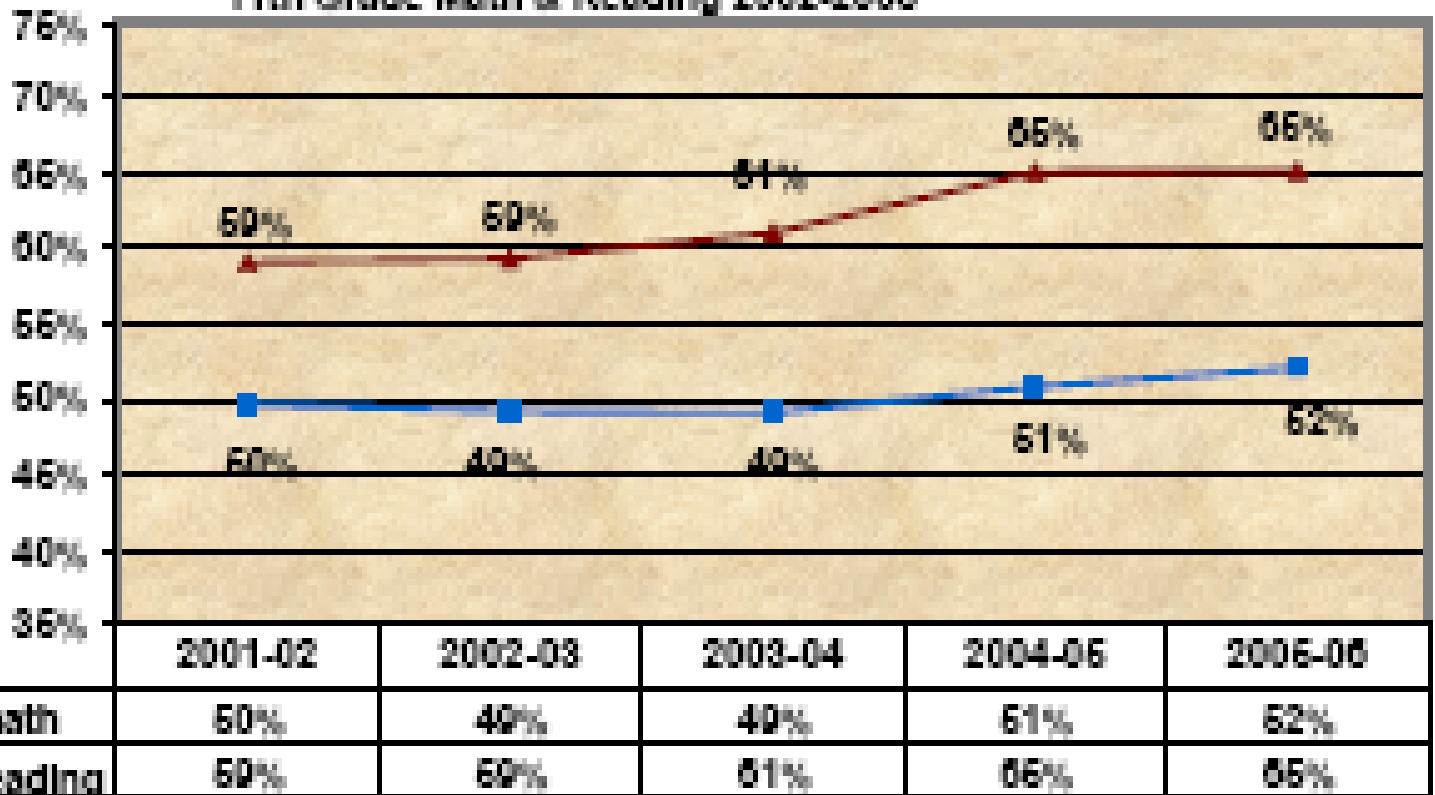
NCLB Mandates Tests versus State Standards in Grades 3-8

Most states stop *nationally normed* tests, and

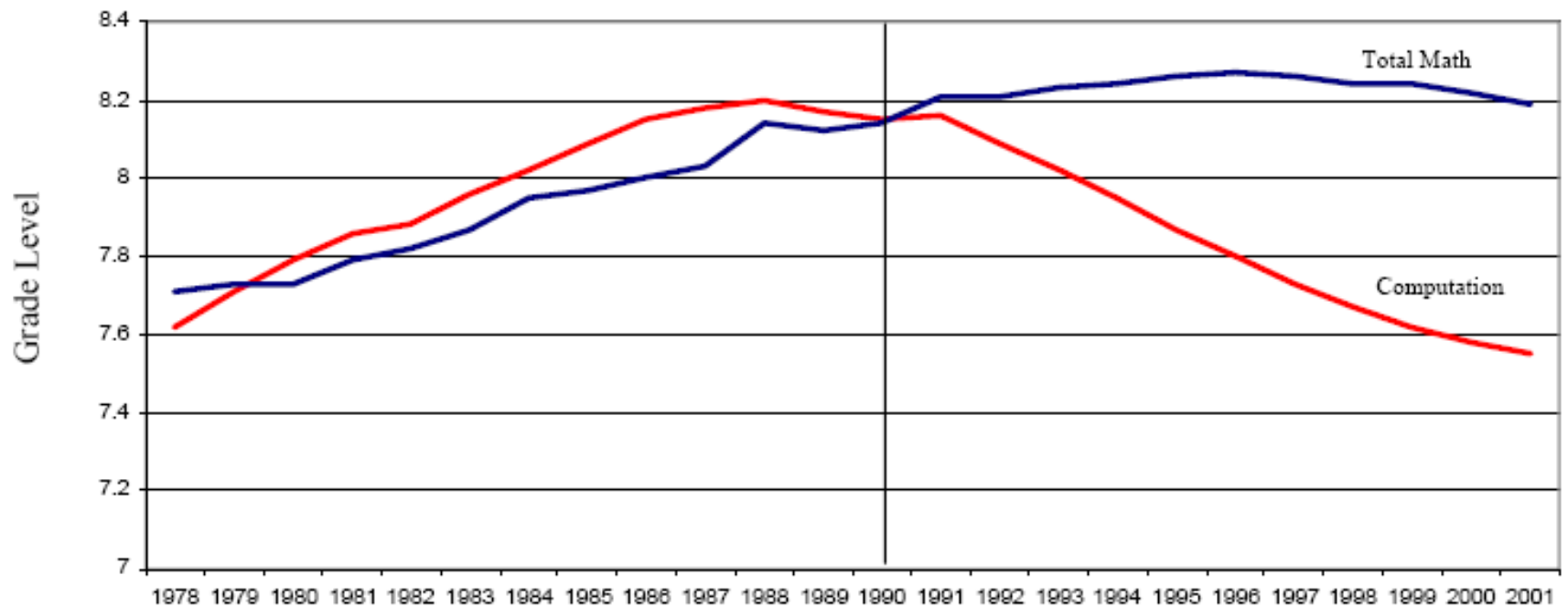
Since 2003 : NO state reports math *computation*

# Pennsylvania:

11th Grade Math & Reading 2002-2006



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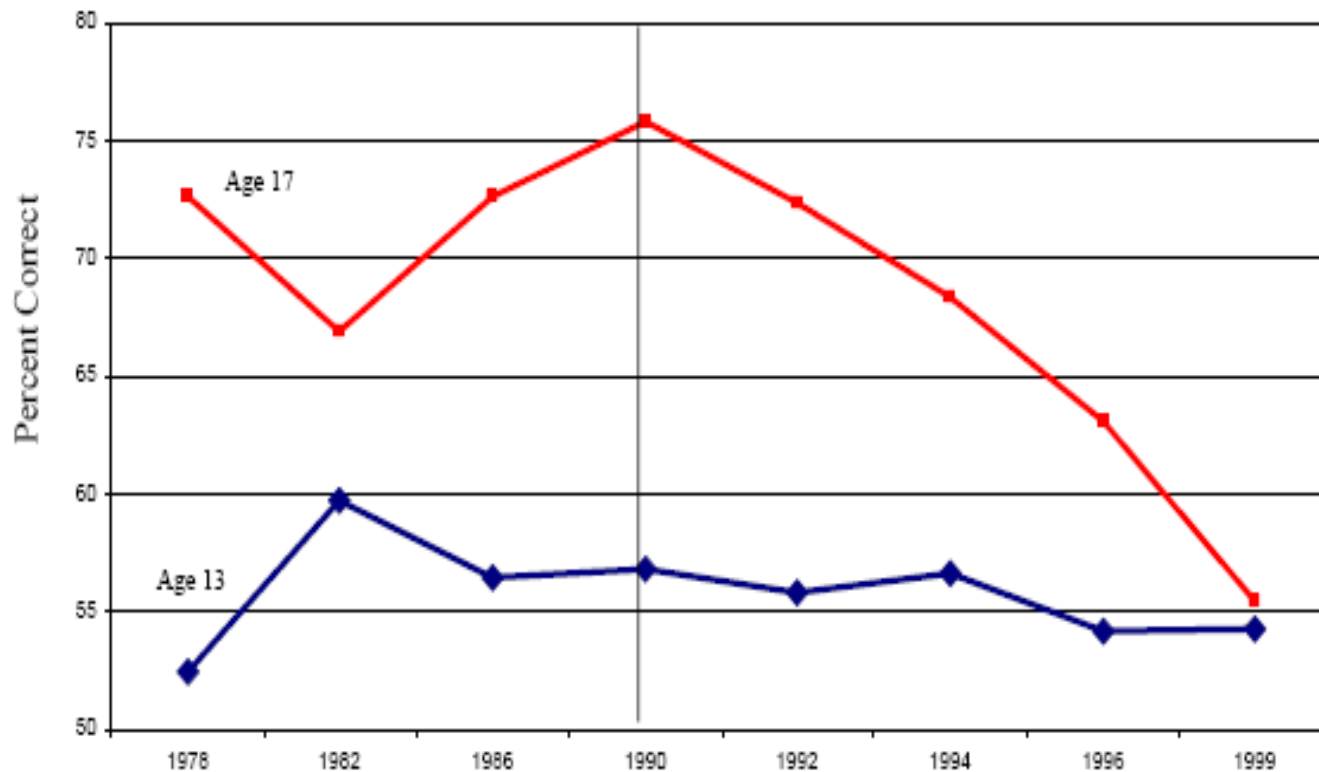
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# 2003 to 2010

- STEM *talk*, but readiness not measured.
- \$\$ Millions/yr spent on state K-12 tests, but
- Computation scores not reported,
- Readiness for chem, physics, engineering?  
Dropped to 2002. Now? No data.

# Was this the students' fault?

## Fractions-- Item Analysis NAEP Long-Term Trend, 1978-1999



# The Bohr Model

How do we  
**FIX**  
the **problem?**

# ~2006: Cognitive Science Says

- You solve problems in Working Memory
- Working memory is VERY limited when manipulating information NOT in Long-Term Memory
- Fast recall of fundamentals (fluency) from Long-Term memory overcomes limits in Working Memory.

**Fix #1:**

**Standards That  
Include Computation:**

**Good News.**

# New K-12 Math Standards

**2010**: National Governor's Assn.  
proposes (& feds push with \$\$\$)

- K-12 “Common Core Standards”
- Non-federal, state voluntary  
“National Standards”

**2010-11**:

**44 states** adopt Common Core stds.

# For a review of the Common Core Math Standards:

- [http://edexcellence.net/doc/20100323\\_CommonCoreReview\\_Math.pdf](http://edexcellence.net/doc/20100323_CommonCoreReview_Math.pdf)

## Good on Computation:

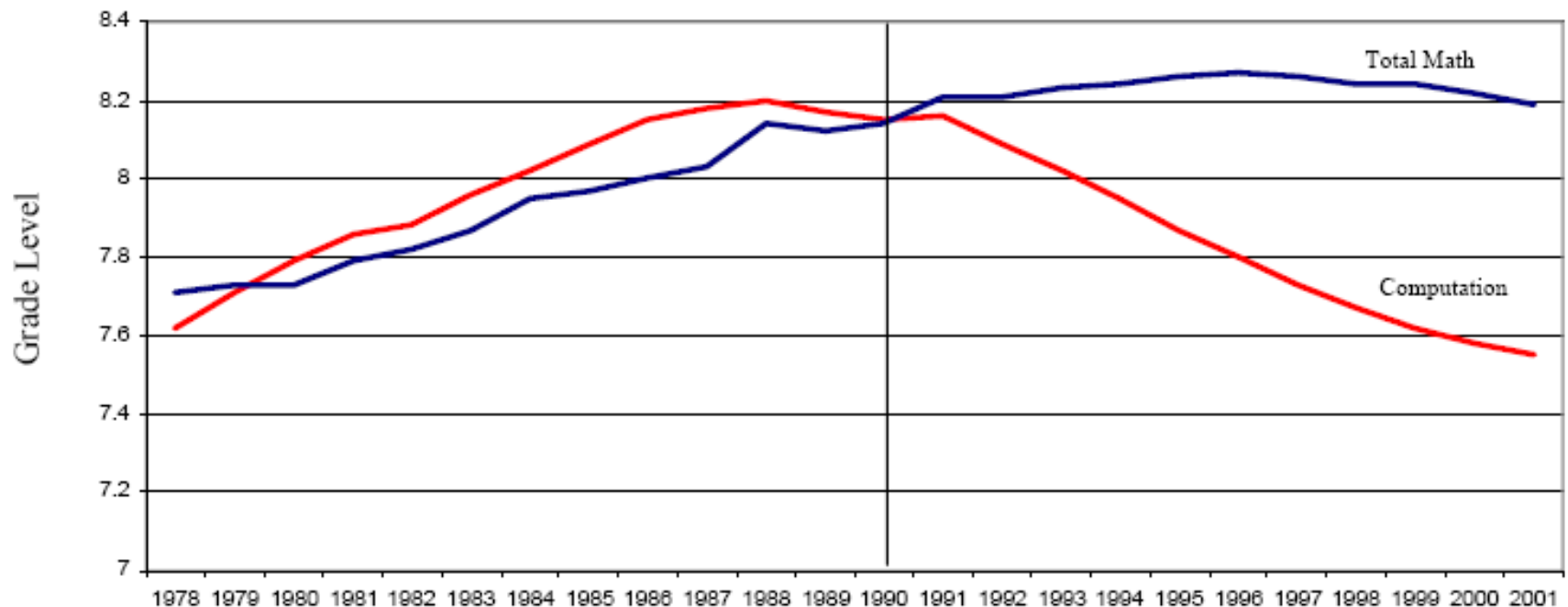
- “By end of Grade 2, fluently add and subtract within 20. Know from memory sums of one-digit numbers.”
- “Fluently ... multiply whole numbers using the standard algorithm....” (Grade 5)
- Fluent means: fast from memory.

# When Will New Standards Help?

- 3 years to get books/tests on new stds.
- 6-10 years of gradual K-12 text purchase
- Students caught in abrupt transition
- 10+ years to put students through under new standards.

**Not for 10-20 years**

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## Fix #2

- Ask your state to report computation

(versus time, standards, international norms).

Tested = Taught

If Reported = Sooner Fixed

Fix #3:

In Chem, Address the  
Computation Deficits  
While Waiting

# 2011 to 2030

If we want

- more majors
- More Gen Chem success

Offer students practice in math  
pre-requisite for chemistry

**Is this  
Remediation?**

# Computation Teaching Options:

1. Integrate *Computation* instruction and practice into Gen Chem homework.

And/Or

2. One Credit

concurrent with Gen Chem I  
“Prep for *Calculations*”

And/OR

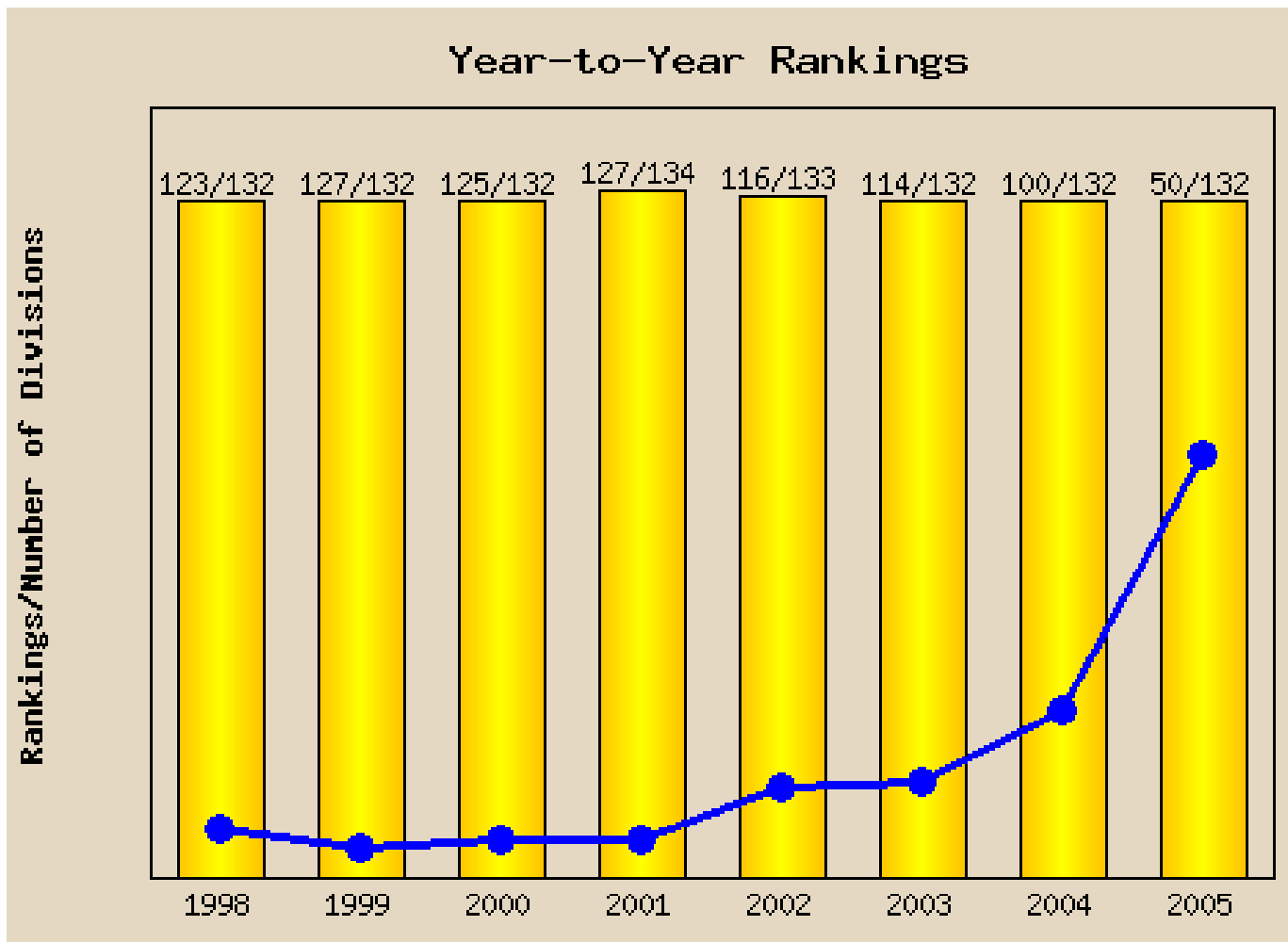
3. 3 Credit “Prep Chem” -- but  
focused on *computation*.

- 1,000 pages of free chem *computation* homework options, with instructor reviews, at [www.ChemReview.Net](http://www.ChemReview.Net)
- Math of chem -- with & **w/o** a calculator

# Can Improved Curriculum Help?

# Good News

Between 2001 and 2005, in 3<sup>rd</sup> Grade Reading, for *all* students, Richmond VA rose from ranking in the bottom 5% to the top 40% of the state, an unprecedented accomplishment for a high-poverty district.





Stanford 9 Results  
1998-2001

PERCENT OF ALL STUDENTS SCORING AT OR ABOVE THE 50TH PERCENTILE

MATHEMATICS TEST						
Grade	1998	1999	2000	2001	CHANGE 1998-2001	COHORT CHANGE
2	43	49	57	58	15	
3	40	48	56	59	19	
4	39	44	51	54	15	
5	41	45	50	55	14	12
6	46	50	55	58	12	18
7	42	45	48	50	8	11
8	42	45	48	49	7	8
9	47	48	51	51	4	5
10	41	44	46	45	4	3
11	43	45	48	46	3	4

# California Science Enrollment

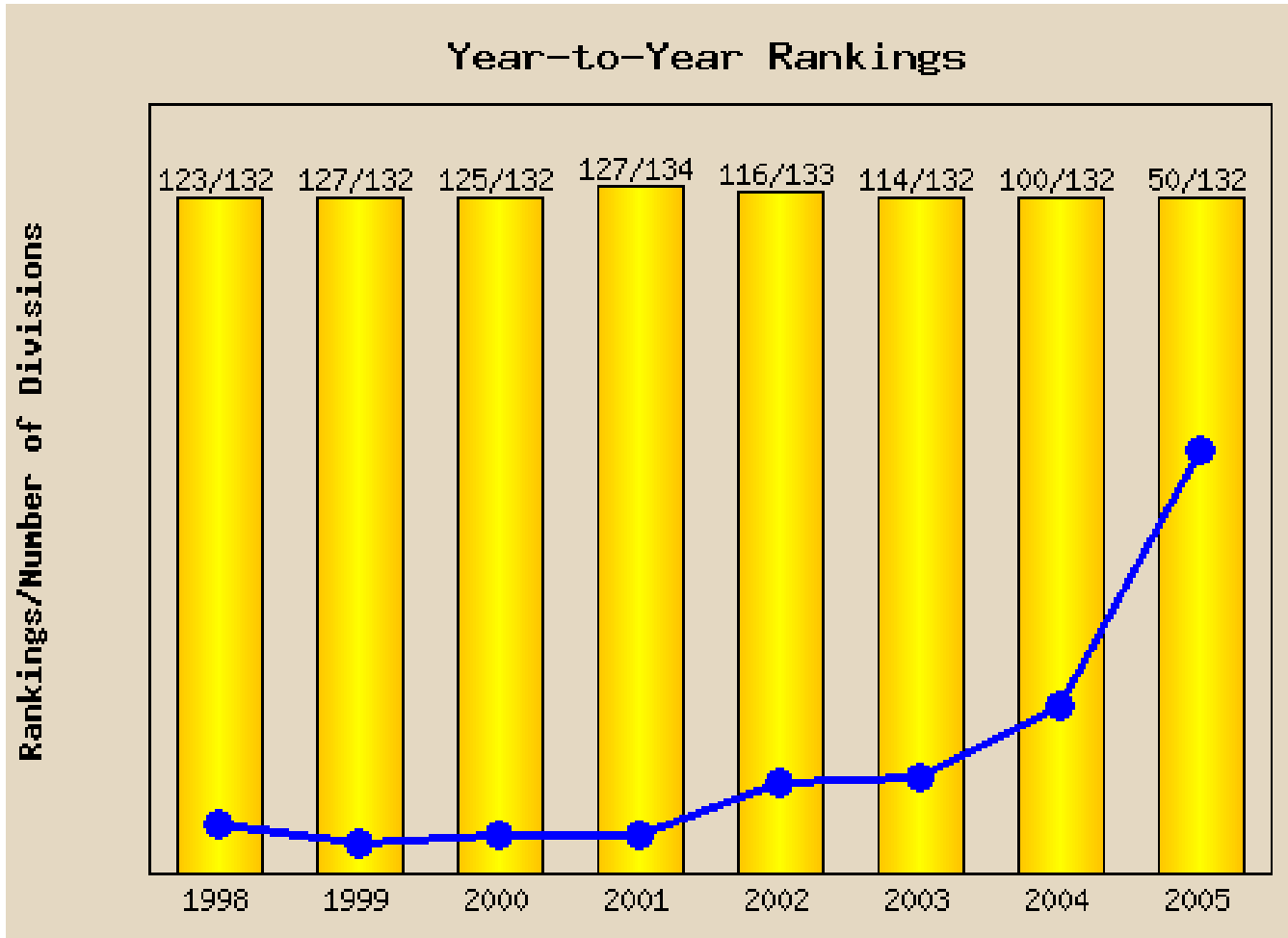
## Science—End-of-Course (Grades Nine Through Eleven)

**Table 12: Numbers of Students Tested\***

Test	2003	2005	2007	2009	Change in Number 2003-2009
Earth Science	89,676	173,958	207,246	226,111	136,435
Biology	334,005	453,685	507,155	534,877	200,872
Chemistry	153,491	196,700	227,866	247,306	93,815
Physics	44,878	59,382	63,450	67,838	22,960

# Using Cognitive Science,

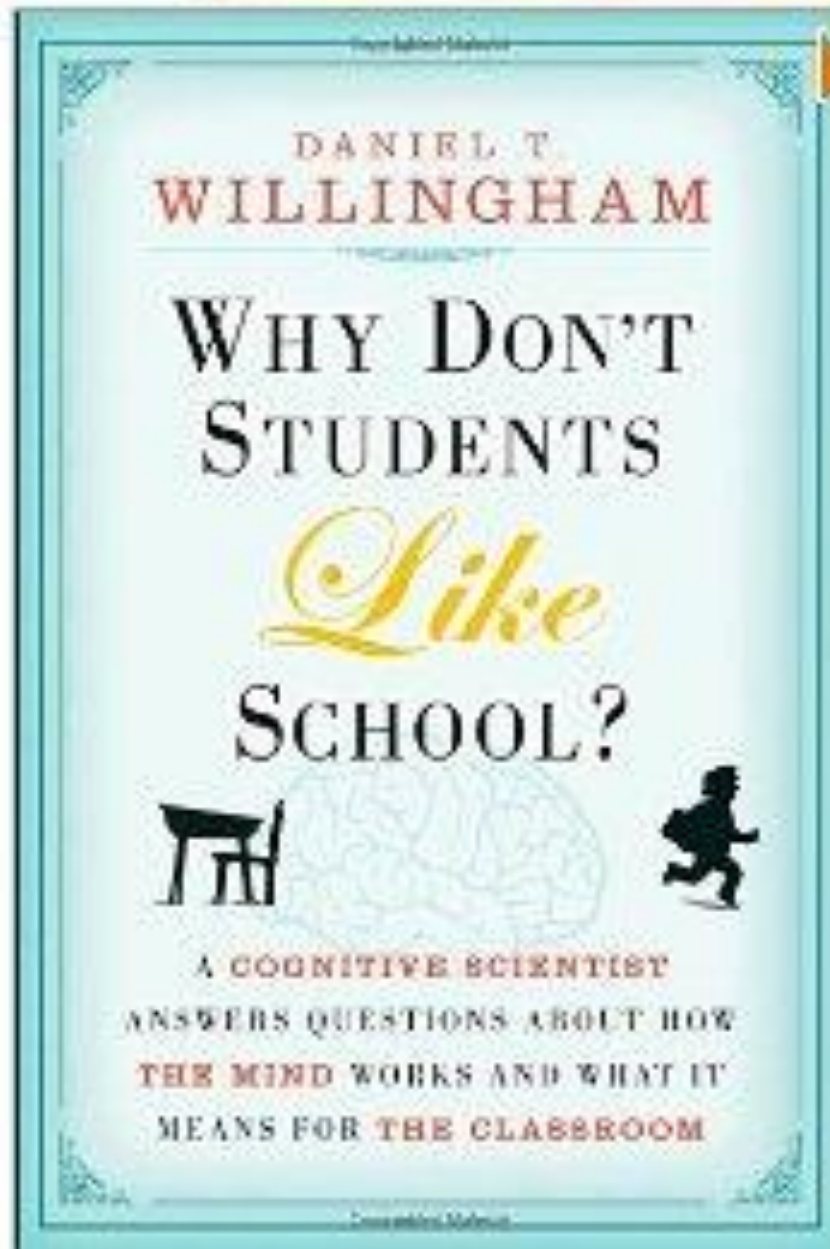
# Achievement Does This:



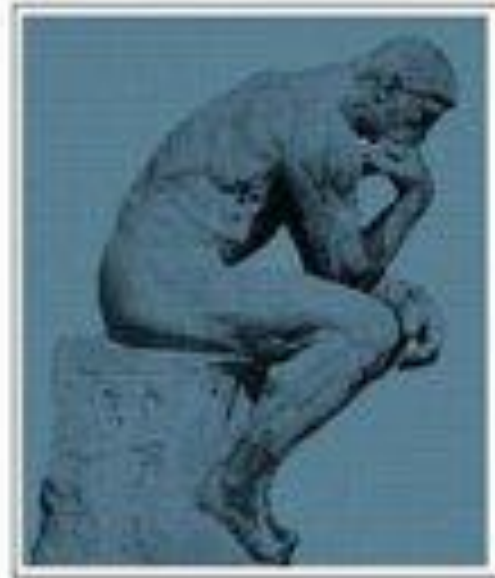
# Chemistry Education

Click to **LOOK INSIDE!**

# 3 Books on the New Cognitive Science: 1. Easy Read



**2.  
Cog  
Psych  
Textbook**

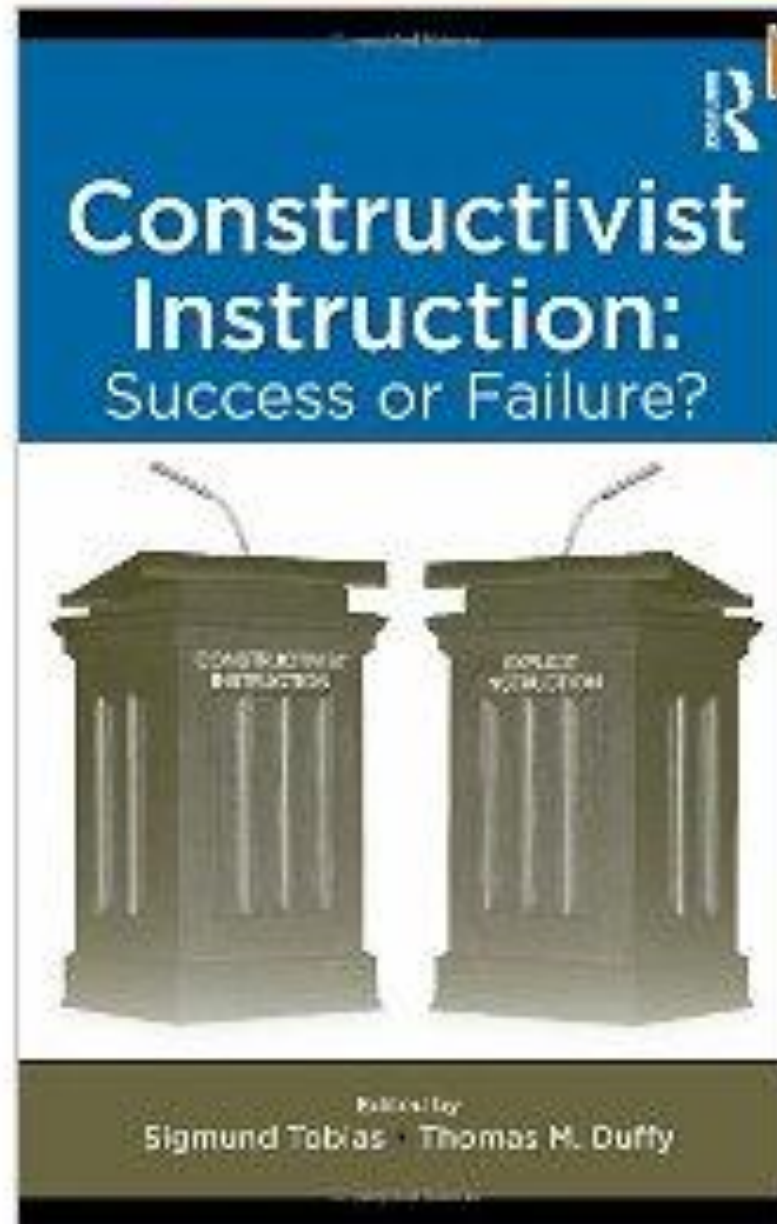


**COGNITION**  
*The Thinking Animal*  
THIRD EDITION

DANIEL T. WILLINGHAM

### 3. Cutting Edge on Theory

Click to **LOOK INSIDE!**



# Gen Chem

Gateway to Science and Engineering

that is the

Foundation for America.

We Need Students *Ready*

For Gen Chem

# Summary

- Student Preparation for Chemistry ↓ ↓ ↓
- States De-emphasized K-12 Computation
- Impact on National Economy
- Fixed Standards: Impact 10-20 years out
- Teaching Science-Math falls on us
- New Cognitive Science can help

These slides are posted at  
[www.ChemReview.Net](http://www.ChemReview.Net)  
at the MARM tabs on the left.  
Please feel free to use this data.  
Done! Questions?

Backup and  
Question  
Response  
Slides follow

In your head:

76

x 67

# Solving Problems

The Cognitive Science Model: We use

- Long-term memory (enormous)
- Short-term memory (short and limited)
- Working memory
  - Where we *think* and *solve* problems
  - VERY limited in handling *new* data

# Limited Working Memory

“We can hold no more than about seven *novel* elements (not in LT memory) of information in working memory and can process no more than about 4 elements depending on the nature of the processing required.”

- J. Sweller in *Constructivist Instruction: Success or Failure* (2009), p. 136, citing N. Cowan, The magical number 4 in short-term memory, *Behavior and Brain Sciences*, 24, 87-114

# When Solving a Problem

Working memory can manipulate

- **4 chunks** of **new** information

Plus

- All that can be recalled “with automaticity” from LT Memory.

*Major* factor? Content in LTM

# Overcoming Limits on Working Memory

- Fundamentals of the discipline memorized to automaticity

And

- Memorized algorithms that “chunk” information and processes

# Memorization?

- “Data from the last 30 years lead to a conclusion that is not scientifically challengeable: thinking well requires knowing facts.... The very processes that teachers care about most-critical thinking processes like reasoning and problem solving-are intimately intertwined with factual knowledge that is in long-term memory (not just in the environment).

\*There is one important exception-how experts think. Building expertise actually changes the thought process, but such change takes many years of advanced study.“

-- Daniel Willingham

[http://archive.aft.org/pubs-reports/american\\_educator/issues/spring2009/index.htm](http://archive.aft.org/pubs-reports/american_educator/issues/spring2009/index.htm)

# Cognitive Science recommends

## *Homework*

- Memorization of core facts of discipline
- Practice at applying algorithms

## During Class

- A focus on concepts
- Guided inquiry to build cognitive frameworks and interest
- Do the Shakhashiri